

⑫ **EUROPEAN PATENT APPLICATION**

⑲ Application number: **82109850.6**

⑤① Int. Cl.<sup>3</sup>: **F 01 C 1/16**

⑳ Date of filing: **25.10.82**

④③ Date of publication of application: **02.05.84**  
**Bulletin 84/18**

⑦① Applicant: **Hitachi, Ltd., 5-1, Marunouchi 1-chome,**  
**Chiyoda-ku Tokyo 100 (JP)**

⑦② Inventor: **Kasuya, Katsuhiko, 1993-114, Shimoimayoshi**  
**Chiyodamura, Niihari-gun Ibaraki-ken (JP)**  
Inventor: **Mori, Hidetomo, 195-2, Asahicho**  
**Tomobemachi, Nishibaraki-gun Ibaraki-ken (JP)**  
Inventor: **Fujiwara, Mitsuru, 2361-8, Oaza Anjiki**  
**Dejimamura, Niihari-gun Ibaraki-ken (JP)**  
Inventor: **Matsunaga, Tetsuzo, 85-14, Shoen,**  
**Sakuramura, Niihari-gun Ibaraki-ken (JP)**

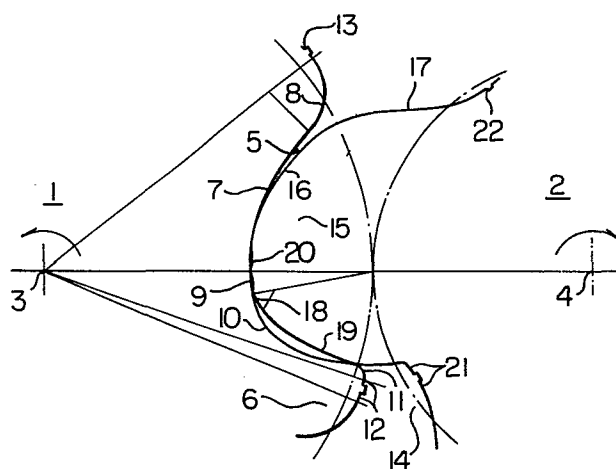
⑧④ Designated Contracting States: **DE FR GB IT NL SE**

⑦④ Representative: **Finck, Dieter et al, Patentanwälte v.**  
**Füner, Ebbinghaus, Finck Marienhilfplatz 2 & 3,**  
**D-8000 München 90 (DE)**

⑤④ **Screw rotor.**

⑤⑦ A pair of screw rotors in the form of a female rotor and a male rotor, wherein, by taking deformation of the rotor due to thermal expansion during operation into consideration, the female rotor has a rotor tooth form including a flank of a surface of advance constituted by an arc (7) and a second order curve, and a flank of a surface of retrocession (10) constituted by a curve generated by an arc (18) of a forward end portion of a robe on the male rotor and an arc, and the male rotor has a rotor tooth form essentially formed by generating loci of the flank of the surface of advance of the female rotor and the flank of the surface of retrocession thereof.

In addition to the influences exerted by the thermal expansion, the backlash of synchronizing means may be taken into consideration in deciding the rotor tooth forms.



SCREW ROTOR

1 BACKGROUND OF THE INVENTION

FIELD OF THE INVENTION

This invention relates to screw rotors of screw compressors, and more particularly it deals with  
5 a pair of screw rotors suitable for use with a dry type screw compressor, blower, expander, etc., in which the rotors rotate while in meshing engagement with each other by using synchronizing means without being brought into contact with each other.

10 Generally, in oilless type screw compressors for use in applications where mingling of oil in the gas discharged from a screw compressor is not desirable, transmission of rotation between screw rotors forming a pair is effected through synchronizing means mounted  
15 at shaft portions outside the working chambers of the rotors, and at this time the rotors rotate while meshing with each other without coming into contact with each other. The screw rotors of this type of screw compressors have a greater chance of the gas leaking from  
20 between the rotors and the casing and between the rotors and from the blowholes than the screw rotors of screw compressors of the oil-cooled type in which the oil is injected into the working chambers in which the rotors mesh with each other to effect lubrication and  
25 cooling of the rotors and provide a seal to the rotors.

1 As a result, the size of the clearance and the blowholes  
exert great influences on the efficiency of the com-  
pressors. In view of this fact, there has been a demand  
for a high degree of accuracy and precision with which  
5 the rotors are shaped and for a rotor tooth form of  
small blowholes.

In the screw rotors of this type of screw  
compressors, the teeth of the rotors have their tem-  
peratures raised to a high level during operation and  
10 are consequently greatly deformed during operation as  
compared with the rotor teeth in normal temperature  
during an inoperative period. Thus, in designing the  
shape of the two rotors of a screw compressor, it is  
necessary not only to take into consideration the  
15 dimensions of the rotors to provide clearances between  
the rotors and between the rotors and the casing in  
such a manner that the rotors are not brought into  
contact with each other during operation and yet the  
clearance is minimized, but also to provide means for  
20 avoiding the occurrence of seizure between the rotors  
and the casing.

Heretofore, it has been usual practice to  
decide, in designing screw rotors, a clearance between  
the two rotors and a clearance between the rotors and  
25 the casing based on a casual idea, and consequently  
the clearances formed have had no theoretical basis.  
This has given rise to a number of problems with  
regard to the operation efficiency of the screw

1 compressors that have remained unsolved.

More specifically, as a process for imparting  
a clearance between the two rotors, proposals have been  
made to use a male rotor as a reference for providing  
5 a basic tooth form of the rotors and a clearance of a  
predetermined size is provided in the direction normal  
to the female rotor tooth form by taking into considera-  
tion deformation and other factors that might possibly  
be caused to occur by thermal expansion during opera-  
10 tion. The screw rotors produced by this process have  
already been put to practical use.

In view of the fact, however, that deformation  
of the tooth form on account of thermal expansion may  
vary depending on the shape of the tooth form, the value  
15 of the clearance decided by the process described  
hereinabove would not be considered an optimum value  
that is obtained by careful analysis of the condition  
of the rotors expanded by heat and of the condition of  
the clearance during operation.

20 In another process for imparting a clearance  
to the two rotors of a screw compressor that is also  
known in the art, a small clearance is provided to a  
region in which the relative sliding movement between  
the two rotor teeth meshing with each other is small  
25 and a sufficiently large clearance is provided to other  
regions of the rotor teeth. This process is disclosed  
in U.S. Patent Specification No. 3,414,189, for example.

This process could not, however, be considered

1 to take the thermal deformation of the two rotors into  
consideration quantitatively in providing a clearance  
to between the rotor.

#### SUMMARY OF THE INVENTION

##### 5 OBJECT OF THE INVENTION

An object of this invention is to provide a  
pair of screw rotors wherein a minimum clearance can  
be provided through the entire region of the teeth of  
the female rotor and the male rotor in meshing engage-  
10 ment with each other during operation to thereby greatly  
improve performance.

Another object is to provide a pair of screw  
rotors wherein the female rotor and the male rotor are  
constructed by taking into consideration the backlash  
15 of the synchronizing gears to avoid seizing on account  
of contact of the two rotors during operation, to thereby  
improve the reliability of the screw compressor.

Still another object is to provide a pair of  
screw rotors capable of greatly improving performance  
20 by taking into consideration the axial temperature  
distribution inside and outside the rotors when they  
are constructed.

A further object is to provide a pair of screw  
rotors capable of greatly prolonging the service life  
25 of the tools used for producing the screw rotor and  
having a reduced area of blowholes.

To accomplish the aforesaid objects, the

1 invention provides the following outstanding character-  
istics. One of them is that novel tooth forms are  
imparted to a female rotor and a male rotor rotating  
about two axes parallel to each other and forming a  
5 pair of screw rotors as follows: the flank of the surface  
of advance of the female rotor is constituted by a first  
flank of the surface of advance formed by a second order  
curve, and a second flank of the surface of advance formed  
by an arc of an imaginary circle of a radius  $R_1$  having  
10 its center in the pitch circle of the female rotor in  
normal temperature condition. The flank of the surface  
of retrocession of the female rotor is constituted by  
a first flank of the surface of retrocession generated  
by a forward end portion of a robe of the male rotor  
15 formed by an arc of an imaginary circle of a radius  
 $R_4$  having its center on a line drawn from the pitch  
point which is inclined through an angle  $\phi$  with respect  
to a straight line connecting the two axes together,  
and a second flank of the surface of retrocession  
20 formed by an arc of an imaginary circle of a radius  $R_3$   
of an imaginary circle having its center in the pitch  
circle of the female rotor. The male rotor is essential-  
ly formed by generating loci of the flank of the surface  
of advance of the female rotor and the flank of the  
25 surface of retrocession thereof, to thereby provide  
basic tooth forms of the female rotor and the male rotor.  
One of the basic tooth forms of the female and male  
rotors is used as one rotor tooth form, and a rotor

1 tooth form is obtained from the one basic tooth form by  
deformation caused by thermal expansion during operation  
of the rotors. Another rotor tooth form is generated  
based on the thermally deformed tooth form and, and a  
5 normal temperature version of the generated thermally  
deformed tooth form is produced and used as the other  
rotor tooth form.

Another outstanding characteristic is that  
novel tooth forms are imparted to a female rotor and  
10 a male rotor rotating about two axes parallel to each  
other and forming a pair of screw rotors as follows:  
the flank of the surface of advance of the female rotor  
is constituted by a first flank of the surface of  
advance formed by a second order curve, and a second  
15 flank of the surface of advance formed by an arc of an  
imaginary circle of a radius  $R_1$  having its center in  
the pitch circle of the female rotor in normal tempera-  
ture condition. The flank of the surface of retrocession  
of the female rotor is constituted by a first flank of  
20 the surface of retrocession generated by a forward end  
portion of a robe of the male rotor formed by an arc  
of an imaginary circle of a radius  $R_4$  having its  
center on a line drawn from the pitch point which is  
inclined through an angle  $\phi$  with respect to a straight  
25 line connecting the two axes together, and a second  
flank of the surface of retrocession formed by an arc  
of an imaginary circle of a radius  $R_3$  of an imaginary  
circle having its center in the pitch circle of the

- 1 female rotor. The male rotor is essentially formed by  
generating loci of the flank of the surface of advance  
of the female rotor and the flank of the surface of  
retrocession thereof, to thereby provide basic tooth  
5 forms of the female rotor and the male rotor. One of  
the basic forms of the female and male rotors is used  
as one rotor tooth form, and a rotor tooth form of the  
one basic tooth form that is deformed by thermal  
expansion during operation of the rotors is obtained.
- 10 Then another rotor tooth form is generated based on the  
thermally deformed tooth form, and a rotor tooth form  
is obtained by reducing an amount corresponding to the  
backlash of synchronizing means from the another tooth  
form. A normal temperature version of this rotor tooth  
15 form is used as the other tooth form.

Still another outstanding characteristic is  
that novel tooth forms are imparted to a female rotor  
and a male rotor rotating about two axes parallel to  
each other and forming a pair of rotor screws as follows:

20 the flank of the surface of advance of the female rotor  
is constituted by a first flank of the surface of  
advance formed by a second order curve, and a second  
flank of the surface of advance formed by an arc of  
an imaginary circle of a radius  $R_1$  having its center  
25 in the pitch circle of the female rotor in normal tem-  
perature condition. The flank of the surface of retro-  
cession of the female rotor is constituted by a first  
flank of the surface of retrocession generated by a



1 forward end portion of a robe of the male rotor  
formed by an arc of an imaginary circle of a radius  $R_4$   
having its center on a line drawn from the pitch point  
which is inclined through an angle  $\phi$  with respect to  
5 a straight line connecting the two axes together, and  
a second flank of the surface of retrocession formed by  
an arc of an imaginary circle of a radius  $R_3$  of an  
imaginary circle having its center in the pitch circle  
of the female rotor. The male rotor is essentially  
10 formed by generating loci of the flank of the surface  
of advance of the female rotor and the flank of the  
surface of retrocession thereof, to thereby provide  
basic tooth forms of the female and male rotors. One  
of the basic tooth forms of the female and male rotors  
15 is used as one rotor tooth form, and a rotor tooth  
form is obtained by adding to the one rotor tooth form  
an amount corresponding to the thermal expansion of the  
rotor and the backlash of the synchronizing means  
occurring during operation of the rotor. The rotor  
20 tooth form thus produced is used for generating the  
other tooth form from which a normal temperature  
version of the other rotor tooth form is obtained.

#### BRIEF DESCRIPTION OF THE DRAWINGS

Fig. 1 is a sectional view perpendicular to  
25 the axis of the basic tooth forms of the screw rotors  
comprising a first embodiment of the invention;

Fig. 2 is a view similar to Fig. 1 but shown

1 on an enlarged scale;

Fig. 3 is a view of the details of the tip  
of the tooth top of the male rotor;

Fig. 4 is a sectional view perpendicular to  
5 the axis of the basic tooth forms of the screw rotors  
comprising a second embodiment;

Fig. 5 is a view in explanation of the basic  
tooth forms of the screw rotors according to the  
invention;

10 Figs. 6-9 are views showing the first embodi-  
ment of the screw rotors in conformity with the invention  
in which thermal expansion is taken into consideration,  
in explanation of the process for obtaining the tooth  
forms for the screw rotors;

15 Figs. 10 and 11 are views showing the second  
embodiment of the screw rotors in conformity with the  
invention in which thermal expansion is taken into  
consideration, in explanation of the process for obtaining  
the tooth forms for the screw rotors;

20 Figs. 12 and 13 are views showing the third  
embodiment of the screw rotors in conformity with the  
invention in which thermal expansion is taken into  
consideration, in explanation of the process for  
obtaining the tooth forms for the screw rotors; and

25 Fig. 14 is a side view of a screw rotor  
representing a modification of the embodiments of the  
invention.

1 DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

One embodiment of the basic tooth forms of the screw rotors according to the invencion will be described. Referring to Fig. 1, a female rotor 1 and  
5 a male rotor 2 are in meshing engagement with each other. The two rotors 1 and 2 have their centers of rotation at 3 and 4 respectively for rotation in a casing, not shown, in the directions of arrows, so as to function as a compressor. The two rotors 1 and 2  
10 have synchronizing means, not shown, mounted at their respective shafts outside working chambers, to enable the rotors 1 and 2 to rotate while a small clearance is being maintained therebetween without coming into contact with each other.

15 In normal temperature condition, the female rotor 1 is formed with a plurality of grooves 5 and robes 6. The surface of advance of each groove 5 is constituted by a first flank 7 and a second flank 8, while the surface of retrocession of each groove 5  
20 is constituted by a tooth root flank 9, a first flank 10 and a second flank 11. The tooth top of each robes 6 is constituted by an outer peripheral flank 12 and a tooth top tip 13. Meanwhile the male rotor 2 is formed with a plurality of grooves 14 and robes 15. The surface  
25 of advance of each robe 15 is constituted by a first flank 16 and a second flank 17, and the surface of retrocession thereof is constituted by a first flank 18 and a second flank 19. The forward end of each robe

1 15 is constituted by a tooth top tip 20, and the tooth  
root of each groove 14 is constituted by a tooth root  
flank 21 and a recess 22.

Fig. 2 shows the rotors 1 and 2 on an enlarged  
5 scale. In the surface of advance of the female rotor  
1, a section 25-26 of the first flank 7 is formed by  
a parabola, one kind of a second order curve, focused  
on a point 28 on a straight line connecting the centers  
3 and 4 of the two rotors 1 and 2 together. A section  
10 26-29 of the second flank 8 is formed by an arc of an  
imaginary circle of a radius  $R_1$  centered at a point 30  
inside a pitch circle 23. In the surface of retroces-  
sion of the female rotor 1, a section 25-31 of the  
tooth root flank 9 is formed by an arc of an imaginary  
15 circle of a radius  $R_2$  centered at a pitch point 32, and  
a section 31-35 of the first flank 10 is formed as a  
locus generated by the first flank 18 of the surface  
of retrocession of the male rotor 2 formed by an arc  
of an imaginary circle of a radius  $R_4$  centered at a  
20 point 34 on a line 33 inclined through an angle  $\phi$  with  
respect to a straight line connecting the centers 3 and  
4 of the two rotors 1 and 2 together. A section 35-36  
of the second flank 11 of the surface of retrocession  
of the female rotor 1 is formed by an arc of an imaginary  
25 circle of a radius  $R_3$  smaller than the radius  $R_1$  of  
the imaginary circle forming the second flank 8 of the  
surface of advance and centered at a point 37 inside  
the pitch circle 23.

1 By forming the second flank 8 of the surface  
of advance of the female rotor 1 by the arc of the  
imaginary circle of the radius  $R_1$  which is greater than  
the radius  $R_3$  of the imaginary circle of the arc forming  
5 the second flank 11 of the surface of retrocession of  
the female rotor 1, it is possible to greatly prolong  
the service life of the cutting blade of a hob for  
working on the rotors and to use an inexpensive material  
for producing the cutting blade of the hob with preci-  
10 sion finishes. Thus it is possible to produce the  
rotors by using a hob with a cutting blade of high  
precision finishes, so that the precision with which  
the rotors can be produced is increased and the per-  
formance of the compressor can be greatly improved.  
15 Since the radius  $R_3$  of the imaginary circle of the arc  
for forming the second flank 11 of the surface of  
retrocession is small, the blowholes have a small area  
and leaks of gas are reduced, to thereby improve the  
performance of the compressor.

20 By forming the first flank 7 of the surface  
of advance by a secondary curve of parabola, it is  
possible to lower the rate of slipping occurring when  
the female rotor 1 is driven by the male rotor 2. This  
is conducive to a reduction in wear caused on the two  
25 rotors 1 and 2 and a mechanical loss suffered as by  
bearings of the rotors.

Referring to Fig. 2 again, a section 36-29  
of the outer peripheral flank 12 of each robe 6 of the

1 female rotor 1 is formed by an arc of an imaginary circle  
having its center at the aforesaid center 3 except for  
an elevated portion of the tooth top tip 13.

Meanwhile in the surface of advance of the  
5 male rotor 2, a section 38-39 of the first flank 16 is  
of a shape generated by the first flank 7 of the surface  
of advance of the female rotor 1, and a section 39-40  
of the second flank 17 is of a shape generated by the  
second flank 8 of the surface of advance of the female  
10 rotor 1. A section 41-42 of the first flank 18 of the  
surface of retrocession is formed by the aforesaid arc  
of the imaginary circle of the radius  $R_4$  centered at  
the point 34, and a section 42-43 of the second flank  
19 is generated by the second flank 11 of the surface  
15 of retrocession of the female rotor 1. A forward end  
of each robe 15 is formed by the tooth top tip 20, and  
a section 40-43 of the tooth root flank 21 is formed  
by an arc of an imaginary circle having its center at  
the center point 4 of the male rotor 2 except for the  
20 recess 22 which is formed as a groove of a size large  
enough to receive the tooth top tip 13 of the female  
rotor 1.

Fig. 3 shows in detail the tooth top tip 20  
of the male rotor 2. The tooth top tip 20 of the male  
25 rotor 2 is formed with a section indicated by a solid  
line 41-44-45-38, and the shape of the tooth top tip  
20 is a tip form that can be generated when the male  
rotor 2 is produced by hobbing.

1 By forming at the forward end of the robe on  
the female rotor 1 and the male rotor 2 tooth top tips  
13 and 20 of a shape that can best be produced by  
hobbing, it is possible to produce screw rotors by  
5 relying on hobbing alone for forming all the shapes  
of the rotors. This is conducive to improved produc-  
tivity. The provision of the tooth top tips enables  
seizure between the rotors and the casing to be avoided,  
thereby improving the reliability of compressor.

10 Fig. 4 shows another embodiment of the inven-  
tion in which the first flank of the surface of advance  
of the female rotor of the screw rotors shown in Figs.  
1-3 is modified. In the figure, parts similar to those  
shown in Figs. 1-3 are designed by like reference  
15 characters.

The numeral 46 designates a first flank of  
the surface of advance of the female rotor formed by  
an arc of a second order curve which extends from a  
point 26 to a point 47. The section 26-47 is formed by  
20 an arc of an imaginary circle of a radius  $R_5$  having its  
center 48 outside the pitch circle 23 of the female  
rotor 1. A section 25-47 is formed by an arc of an  
imaginary circle having its center at a point of inter-  
section between the pitch circles 23 and 24.

25 By forming the first flank of the surface of  
advance by an arc, it is possible to increase the  
pressure angle of the cutting blade of a hob, thereby  
facilitating hobbing.

1           A first embodiment of the screw rotors in  
conformity with the invention in which thermal expansion  
is taken into consideration will now be described by  
referring to the drawings.

5           In Fig. 5, parts similar to those shown in  
Figs. 1-4 are designated by like reference characters.  
In the figure, the numerals 49 and 50 designate basic  
tooth forms of the female rotor 1 and the male rotor 2  
respectively. The rotor tooth forms 49 and 50 are such  
10 that they are in meshing engagement with each other  
without any clearance therebetween in normal temperature  
condition (at about 20° at which the rotors are produced).

Figs. 6-8 show the process for working the  
invention. In the embodiment shown and described  
15 hereinabove, the male rotor 2 is used as a reference  
and imparting of the basic tooth form 50 to the male  
rotor 2 will be described.

In Figs. 6 and 7, the numeral 51 designates a  
rotor tooth form obtained by thermal deformation of the  
20 basic tooth form of the male rotor during operation of  
the rotors 1 and 2. The rotor tooth form 51 obtained  
by deformation caused by thermal expansion can be  
obtained by calculation by a process of finite elements  
or the like based on a temperature distribution obtained  
25 by measuring the temperature in the rotor. The numeral  
52 designates a rotor tooth form of the female rotor 1  
generated by the rotor tooth form 51 of the male rotor  
2 that can be obtained from the rotor tooth form 51



1 that is deformed by thermal expansion.

By returning the rotor tooth form 52 to a normal temperature condition, a rotor tooth form 53 of the female rotor 1 in normal temperature condition  
5 can be obtained. At this time, one has only to obtain the rotor tooth form 53 by the process of finite elements or the like based on a temperature distribution in the female rotor 1 as described hereinabove.

A concrete example of the aforesaid process  
10 will be described in a most simple form.

Assume that a temperature in a cross section of the two rotors perpendicular to the axis under operation is constant, and that thermal expansion of the rotors due to a rise in temperature occurs such  
15 that the rotors expand in a radial direction corresponding to the distance from the center of each rotor to an arbitrarily selected point on the rotor tooth form.

In Fig. 8, a normal to an arbitrarily selected  
20 point 54 on the basic tooth form 50 of the male rotor 2 is 54-55. The point 54 shifts to a point 56 as a result of expansion in the radial direction due to a rise in temperature. At this time, a normal 56-57 to the point 56 moves parallel to the line 54-55, so that  
25 the point 56 exists on the rotor tooth form 51 obtained by thermal deformation of the basic tooth form 50 of the male rotor 2.

Calculation is done in like manner on thermal

1 deformation at various points on the basic tooth form  
50 to obtain the rotor tooth form 51.

Then the rotor tooth form 52 of the female  
rotor 1 generated by the rotor tooth form 51 of the male  
5 rotor 2 obtained by deformation of the basic tooth form  
50 is obtained as follows. As shown in Fig. 9, when the  
point 57 is located on an intersection of the pitch  
circles a point 58 on a rotor tooth form generated by  
the rotor tooth form at the point 56 can be obtained.  
10 The point 58 exists on the rotor tooth form 52.

To change the rotor tooth form 52 back to the  
rotor tooth form 53, one has only to follow, in reverse,  
the steps of the process described hereinabove by  
referring to conversion of the rotor tooth form 50 to  
15 the rotor tooth form 51.

In the present invention, one rotor tooth  
form produced by taking thermal expansion into con-  
sideration is used for generating the other tooth  
form, so that it is possible to maintain a minimum  
20 clearance through the entire region of the tooth forms  
of the female and male rotors 1 and 2 during operation.  
This is conducive to a marked improvement in the  
performance of the screw rotors of the dry type screw  
compressors in operation.

25 Fig. 10 shows a second embodiment of the  
process which is distinct from the first embodiment  
described hereinabove. In Fig. 10, transmission of  
rotation between the female and male rotors 1 and 2 is

1 effected through synchronizing means, such as synchro-  
nizing gears, not shown, located outside the working  
chambers of the rotors 1 and 2. Like the example shown  
in Fig. 9, this example shown in Fig. 10 also uses the  
5 male rotor 2 as a reference and imparts the basic tooth  
form to the male rotor 2.

The numeral 59 designates a rotor tooth form  
obtained from the rotor tooth form 52 of the female  
rotor 1 by reducing the backlash of the synchronizing  
10 gears and the minimum clearance necessary for avoiding  
contacting between the rotors 1 and 2 while they are  
meshing with each other. The numeral 60 designates  
a rotor tooth form obtained by returning the rotor  
tooth form 59 to a normal temperature condition that  
15 can be obtained as by the process of finite elements  
based on a temperature distribution in the female  
rotor 1 as described hereinabove.

The process for obtaining the rotor tooth  
form 59 will be described by referring to Fig. 11. In  
20 Fig. 11, let the sum of the backlash of the synchro-  
nizing gear on the pitch circle 23 of the female rotor  
1 and the necessary minimum clearance between the  
rotors 1 and 2, a length 3-61 of the radius vector at  
an arbitrarily selected point 61 of the rotor tooth  
25 form 52 deformed by thermal expansion, the angle formed  
by the radius vector and the normal to the tooth form  
at the point 61 and the radius from the center point  
3 to the pitch circle 23 be denoted by  $C_o$ ,  $R$ ,  $\alpha$  and  $R_p$

1 respectively. Thus when backlash is taken into con-  
sideration, the point 61 arbitrarily selected on the  
rotor tooth form 52 shifts to a point 62. The distance  
C between the two points 61 and 62 can be expressed by  
5 the following equation:

$$C = \frac{R}{R_p} \cdot C_o \cdot \sin \alpha.$$

By this equation, the rotor tooth form 59  
taking the backlash into consideration can be obtained  
from the rotor tooth form 52 deformed by thermal  
10 expansion.

The rotor tooth form 59 can be converted to  
the rotor tooth form 60 by following, in reverse, the  
steps of the process described hereinabove with reference  
to conversion of the rotor tooth form 50 to the rotor  
15 tooth form 51.

The reason why the backlash is taken into  
consideration is because greater effects can be achieved  
by taking into consideration the backlash of the  
synchronizing gears in obtaining optimum meshing of the  
20 rotors during operation, when such gears are used as  
synchronizing means.

In the invention, the backlash of the synchro-  
nizing gears is taken into consideration when the  
female and male rotors are deformed by thermal expansion  
25 during operation, so that it is possible to keep the  
two rotors from coming into contact with each other

1 during operation. This is conducive to improved  
reliability of the screw compressor. It is possible, of  
course, to improve the performance of the screw com-  
pressor by imparting to the rotors a minimum amount of  
5 backlash in an allowable range of values.

Figs. 12 and 13 show a third embodiment which  
is distinct from the first and second embodiments. In  
Figs. 12 and 13, parts similar to those shown in Figs.  
1-11 are designated by like reference characters.

10 The numeral 63 designates a rotor tooth form  
that takes the backlash into consideration. The rotor  
tooth form 63 represents the rotor tooth form 51  
obtained by deformation due to thermal expansion of the  
basic tooth form 50 plus the backlash of the synchro-  
15 nizing gears and the necessary minimum clearance between  
the rotors for avoiding contacting of the rotors while  
rotating in meshing engagement. The numeral 64  
designates a rotor tooth form of the female rotor 1  
generated by the rotor tooth form 63 that is defined in  
20 consideration of the thermal expansion of the male  
rotor 2 and the backlash of the synchronizing gears,  
and the numeral 65 designates a rotor tooth form of the  
female rotor 1 obtained by returning the rotor tooth  
form 64 to a normal temperature condition.

25 By forming the female rotor 1 and the male  
rotor 2 as described hereinabove, various advantages  
can be offered because the clearance between the two  
rotors is minimized due to their being free from the

1 backlash of the synchronizing gears and to a minimum  
clearance being maintained between them to avoid direct  
contact therebetween. It is thus possible, to minimize  
leaks of the gas, thereby enabling the efficiency of  
5 the screw compressor to be greatly improved.

The clearance between the rotors and the casing  
can be effectively reduced because of the fact that  
thermal deformation of the rotors can be determined  
accurately.

10 In the first, second and third embodiments of  
the invention described hereinabove, the temperature  
distribution in the axial direction of the rotors  
under operation is considered constant. However, in  
actual operating conditions, a temperature gradient of  
15 a substantial degree may exist in the axial direction  
of the rotors depending on the operating conditions  
including the conditions of the working fluid, pressure,  
etc. When the temperature distribution on the suction  
side of low temperature and the temperature distribu-  
20 tion on the discharge side of high temperature are taken  
into consideration, the rotor tooth form is given with  
a shape which tapers or its outer periphery converges  
in going from the suction side (indicated by A) at one  
end of the rotor toward the discharge side (indicated  
25 by B) at the other end thereof, as shown in Fig. 14.

The female rotor 1 or the male rotor 2 or  
both of them may be tapered as shown in Fig. 14.

The second and third embodiments of the

1 invention have been described as being applied to rotors  
of a dry type screw compressors. It is to be understood,  
however, that they may have application in an oil-  
cooled type screw compressors as well.

5           From the foregoing description, it will be  
appreciated that in the screw rotors comprising a  
female rotor and a male rotor according to the invention,  
the tooth form of the female rotor includes a flank  
of the surface of advance constituted by an arc and a  
10 second order curve, and a flank of the surface of  
retrocession constituted by a curve generated by an  
arc located at a forward end portion of a robe of the  
male rotor and an arc, and the tooth form of the male  
rotor is essentially produced by generating the loci  
15 of the flank of the surface of advance of the female  
rotor and the flank of the surface of retrocession  
thereof. This enables a minimum clearance to be  
maintained through the entire region between the tooth  
forms of the female and male rotors meshing with each  
20 other, thereby greatly improving the performance and  
reliability of the screw compressors.

Additional advantages are that the service  
life of the tools can be prolonged and the area of the  
blowholes can be minimized.

WHAT IS CLAIMED IS:

1. A pair of screw rotors comprising a female rotor and a male rotor rotating about two axes parallel to each other, said female screw rotor having a rotor tooth form produced in normal temperature condition  
5 including a flank of a surface of advance comprising a first flank of the surface of advance formed by a second order curve, and a second flank of the surface of advance formed by an arc of an imaginary circle of a radius  $R_1$  having its center in the pitch circle of the  
10 female rotor, and a flank of a surface of retrocession comprising a first flank of the surface of retrocession generated by a forward end portion of a robe on the male rotor formed by an arc of an imaginary circle of a radius  $R_4$  having its center on a line drawn from the  
15 pitch point which is inclined through an angle  $\phi$  with respect to a straight line connecting the two axes together, and a second flank of the surface of retrocession formed by an arc of an imaginary circle of a radius  $R_3$  having its center in the pitch circle of the  
20 female rotor, the male rotor being essentially formed by generating loci of the flank of the surface of advance of the female rotor and the flank of the surface of retrocession thereof, wherein basic tooth forms are provided to the female rotor and the male rotor and one  
25 of the basic tooth forms of the female rotor and the male rotor is used as one rotor tooth form; a rotor tooth form is obtained from said one basic tooth form



by deformation caused by thermal expansion during operation of the rotors; another rotor tooth form is  
30 generated based on the thermally deformed tooth form; and a normal temperature version of the generated thermally deformed tooth form is produced and used as the other rotor tooth form.

2. A pair of screw rotors as claimed in Claim 1, wherein said second order curve forming said first flank of the surface of advance of said female rotor comprises a parabola focused inside the pitch circle of said  
5 female rotor.

3. A pair of screw rotors as claimed in Claim 2, wherein the arc of the imaginary circle of the radius  $R_3$  constituting the second flank of the surface of retrocession of said female rotor is smaller than the  
5 arc of the imaginary circle of the radius  $R_1$  constituting the second flank of the surface of advance of said female rotor.

4. A pair of screw rotors as claimed in Claim 2, wherein said male and female rotors are formed at their outer peripheral portions with elevated portions serving as tooth top tips.

5. A pair of screw rotors as claimed in Claim 1, wherein said second order curve constituting the first flank of the surface of advance of said female rotor comprises an arc of an imaginary circle having its  
5 center outside the pitch circle of said female rotor.

6. A pair of screw rotors as claimed in Claim 5,

wherein the arc of the imaginary circle of the radius  $R_3$  constituting the second flank of the surface of retrocession of said female rotor is smaller than the  
5 arc of the imaginary circle of the radius  $R_1$  constituting the second flank of the surface of advance of said female rotor.

7. A pair of screw rotors as claimed in Claim 5, wherein said male and female rotors are formed at their outer peripheral portions with elevated portions serving as tooth top tips.

8. A pair of screw rotors comprising a female rotor and a male rotor rotating about two axes parallel to each other, said female rotor having a rotor tooth form produced in normal temperature condition including  
5 a flank of a surface of advance comprising a first flank of the surface of advance formed by a second order curve, and a second flank of the surface of advance formed by an arc of an imaginary circle of a radius  $R_1$  having its center in the pitch circle of the  
10 female rotor, and a flank of a surface of retrocession comprising a first flank of the surface of retrocession generated by a forward end portion of a robe on the male rotor formed by a arc of an imaginary circle of a radius  $R_4$  having its center on a line drawn from the  
15 pitch point which is inclined through an angle  $\phi$  with respect to a straight line connecting the two axes together, and a second flank of the surface of retrocession formed by an arc of an imaginary circle of a

radius  $R_3$  having its center in the pitch circle of the  
20 female rotor, the male rotor being essentially formed  
by generating loci of the flank of the surface of advance  
of the female rotor and the flank of the surface of  
retrocession thereof, wherein basic tooth forms are  
provided to the female rotor and the male rotor and one  
25 of the basic tooth forms of the female rotor and the  
male rotor is used as one rotor tooth form; a rotor  
tooth form is obtained from said one basic tooth form  
by deformation caused by thermal expansion during  
operation of the rotors; another rotor tooth form is  
30 generated based on the thermally deformed tooth form;  
another rotor tooth form is obtained from said another  
rotor tooth form by reducing an amount corresponding to  
the backlash of synchronizing means; and a normal  
temperature version of the last mentioned another rotor  
35 tooth form is produced and used as the other tooth form.

9. A pair of screw rotors as claimed in Claim 8,  
wherein said second order curve forming said first  
flank of the surface of advance of said female rotor  
comprises a parabola focused inside the pitch circle  
5 of said female rotor.

10. A pair of screw rotors as claimed in Claim 9,  
wherein the arc of the imaginary circle of the radius  
 $R_3$  constituting the second flank of the surface of  
retrocession of said female rotor is smaller than the  
5 arc of the imaginary circle of the radius  $R_1$  constituting  
the second flank of the surface of advance of said

female rotor.

11. A pair of screw rotors as claimed in Claim 9, wherein said male and female rotors are formed at their outer peripheral portions with elevated portions serving as tooth top tips.

12. A pair of screw rotors as claimed in Claim 8, wherein said second order curve constituting the first flank of the surface of advance of said female rotor comprises an arc of an imaginary circle having its  
5 center outside the pitch circle of said female rotor.

13. A screw rotor as claimed in Claim 12, wherein the arc of the imaginary circle of the radius  $R_3$  constituting the second flank of the surface of retrocession of said female rotor is smaller than the arc of the  
5 imaginary circle of the radius  $R_1$  constituting the second flank of the surface of advance of said female rotor.

14. A pair of screw rotors as claimed in Claim 12, wherein said male and female rotors are formed at their outer peripheral portions with elevated portions serving as tooth top tips.

15. A pair of screw rotors comprising a female rotor and a male rotor rotating about two axes parallel to each other, said female rotor having a rotor tooth form produced in normal temperature condition including  
5 a flank of a surface of advance comprising a first flank of the surface of advance formed by a second order curve, and a second flank of the surface of

advance formed by an arc of an imaginary circle of a  
radius  $R_1$  having its center in the pitch circle of the  
10 female rotor, and a flank of a surface of retrocession  
comprising a first flank of the surface of retrocession  
generated by a forward end portion of a robe on the male  
rotor formed by an arc of an imaginary circle of a  
radius  $R_4$  having its center on a line drawn from the  
15 pitch point which is inclined through an angle  $\phi$  with  
respect to a straight line connecting the two axes  
together, and a second flank of the surface of retro-  
cession formed by an arc of an imaginary circle of a  
radius  $R_3$  having its center in the pitch circle of the  
20 female rotor, the male rotor being essentially formed  
by generating loci of the flank of the surface of  
advance of the female rotor and the flank of the surface  
of retrocession thereof, wherein basic tooth forms  
are provided to the female rotor and the male rotor and  
25 one of the basic tooth forms of the female rotor and  
the male rotor is used as one rotor tooth form; a rotor  
tooth form is obtained from said one basic tooth form  
by adding thereto an amount corresponding to the  
thermal expansion of the rotor and the backlash of  
30 synchronizing means occurring during operation of the  
rotor; another rotor tooth form is generated based on  
the thermally deformed tooth form; and a normal  
temperature version of the generated thermally deformed  
tooth form is produced and used as the other rotor  
35 tooth form.

16. A pair of screw rotors as claimed in Claim 15, wherein said second order curve forming said first flank of the surface of advance of said female rotor comprises a parabola focused inside the pitch circle  
5 of said female rotor.

17. A pair of screw rotors as claimed in Claim 15, wherein the arc of the imaginary circle of the radius  $R_3$  constituting the second flank of the surface of retrocession of said female rotor is smaller than the  
5 arc of the imaginary circle of the radius  $R_1$  constituting the second flank of the surface of advance of said female rotor.

18. A pair of screw rotors as claimed in Claim 16, wherein said male and female rotors are formed at their outer peripheral portions with elevated portions serving as tooth top tips.

19. A pair of screw rotors as claimed in Claim 15, wherein said second order curve constituting the first flank of the surface of advance of said female rotor comprises an arc of an imaginary circle having its  
5 center outside the pitch circle of said female rotor.

20. A pair of screw rotors as claimed in Claim 19, wherein the arc of the imaginary circle of the radius  $R_3$  constituting the second flank of the surface of retrocession of said female rotor is smaller than the  
5 arc of the imaginary circle of the radius  $R_1$  constituting the second flank of the surface of advance of said female rotor.

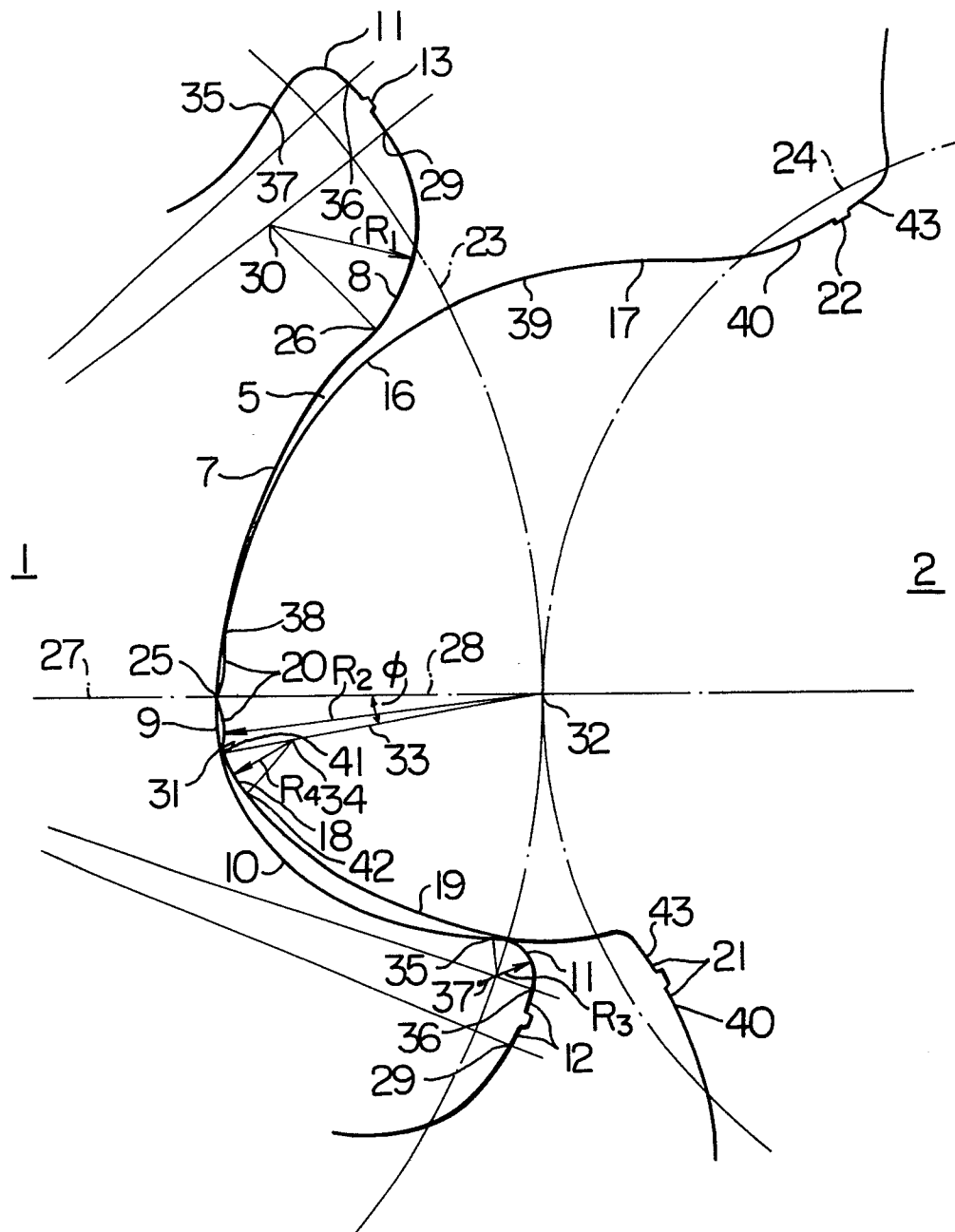
21.           A pair of screw rotors as claimed in Claim 19, wherein said male and female rotors are formed at their outer peripheral portions with elevated portions serving as tooth top tips.

Figure G. 3 is a schematic diagram showing a curved surface profile. The diagram includes the following labeled elements:

- 16**: The main curved surface profile.
- 18**: A dashed line segment representing a radius of curvature.
- 19**: A point on the left side of the curve.
- 20**: A point on the curve, with a bracket indicating a specific region.
- 24**: A point on the right side of the curve.
- 27**: A vertical line passing through the center of curvature.
- 32**: A point at the bottom of the vertical line.
- 34**: A point on the left side of the curve, with a bracket indicating a specific region.
- 38**: A point on the right side of the curve.
- 41**: A point on the left side of the curve.
- 42**: A point on the left side of the curve.
- 44**: A point on the curve.
- 45**: A point on the curve.
- $R_2$** : A radius of curvature from point 32 to point 34.
- $R_4$** : A radius of curvature from point 32 to point 42.
- $\phi$** : An angle between the vertical line 27 and the radius  $R_2$ .



FIG. 2



3/7

FIG. 4

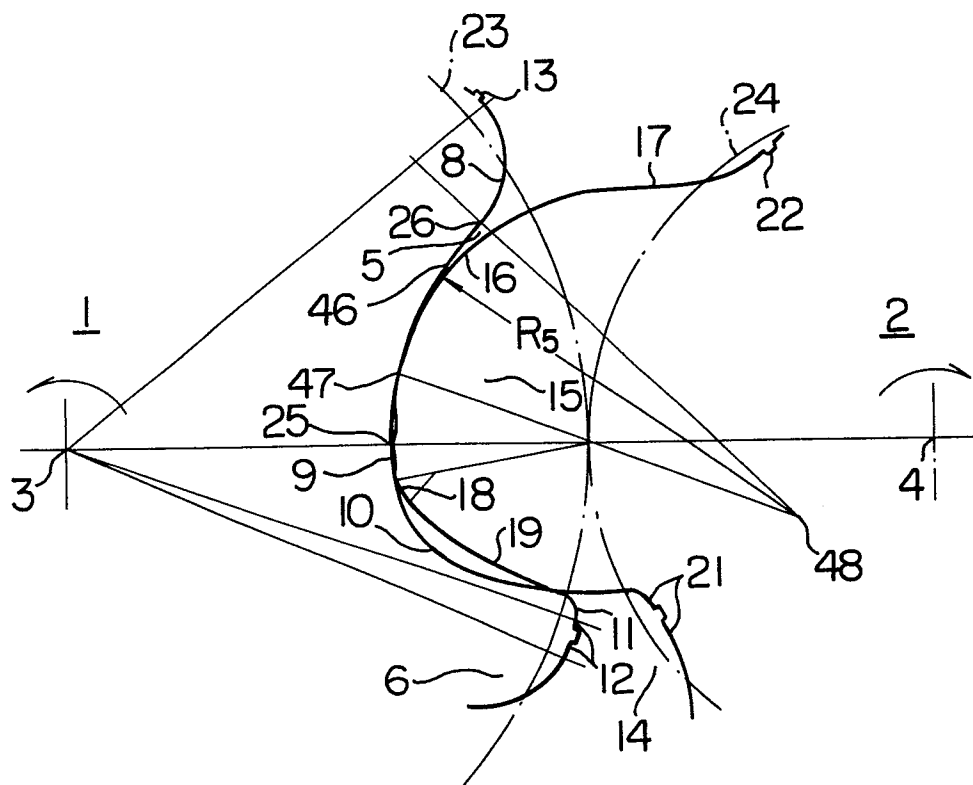


FIG. 5

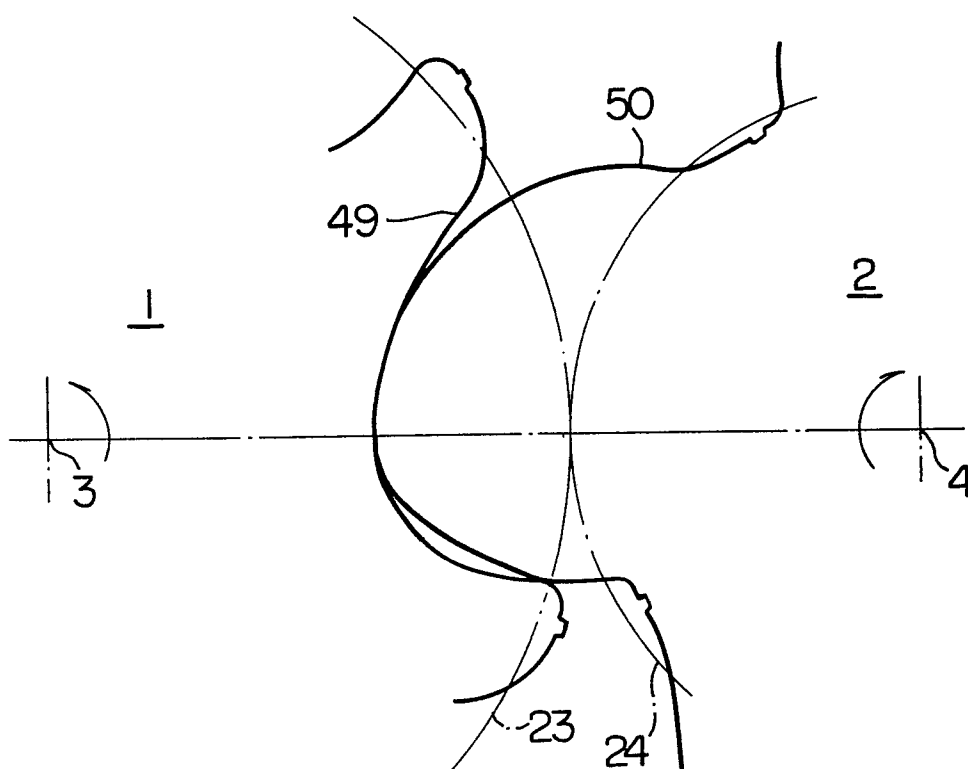


FIG. 6

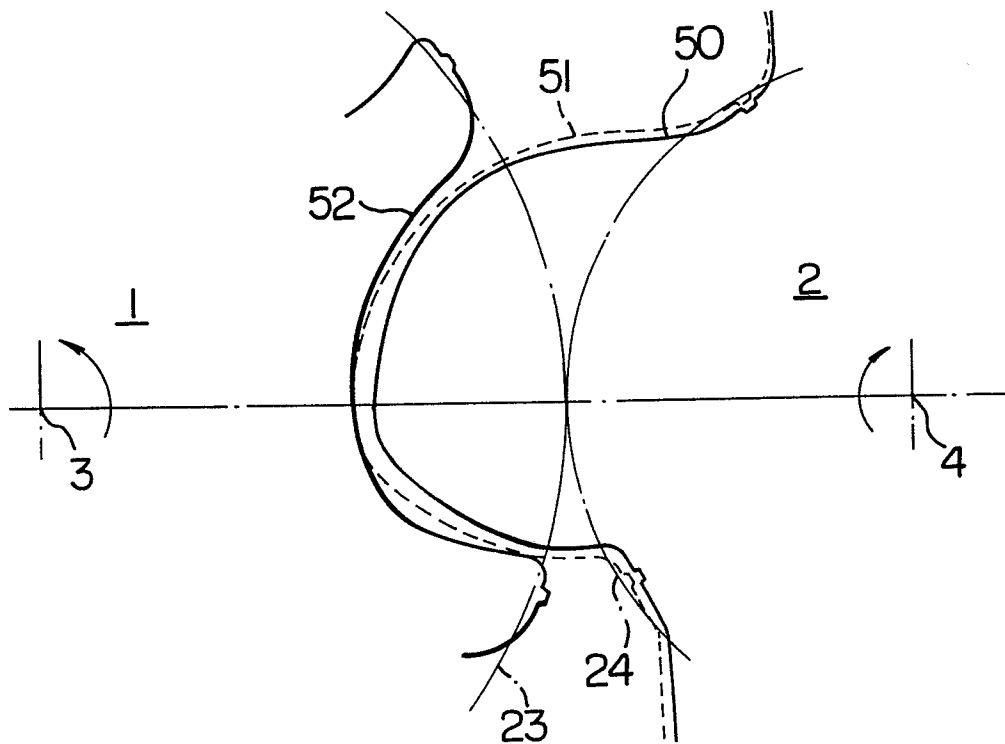
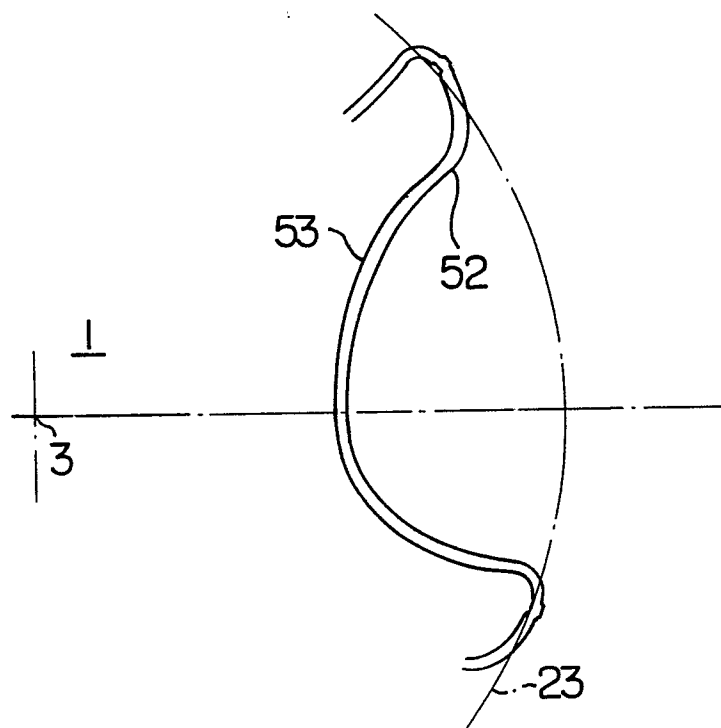


FIG. 7



5/7

FIG. 8

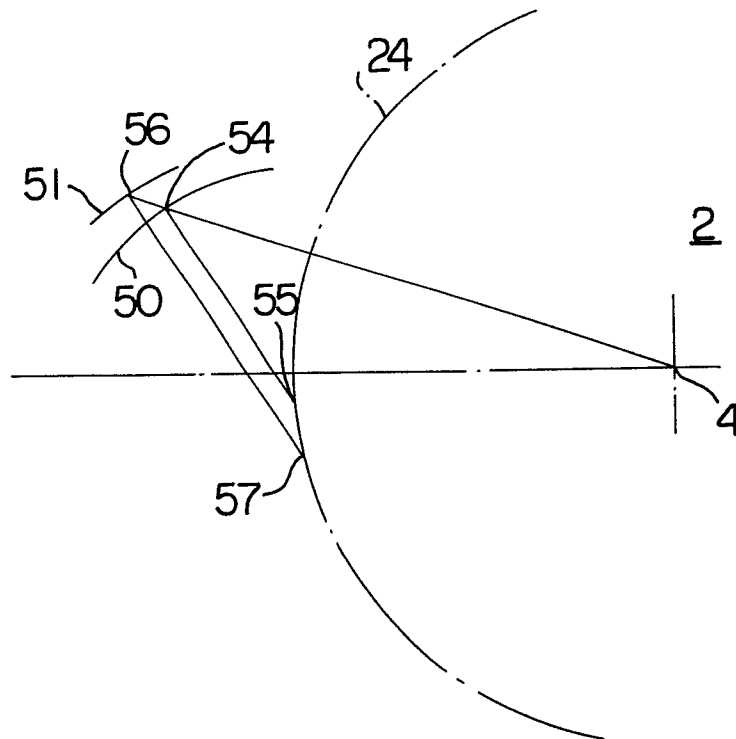
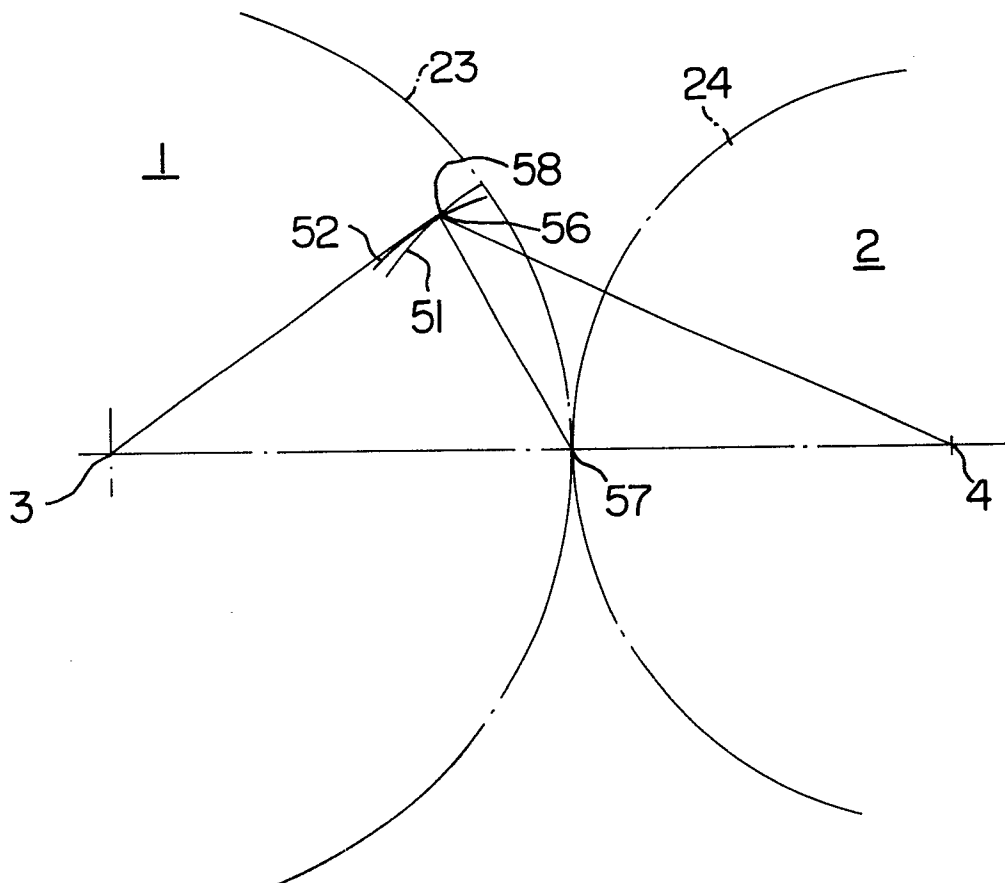


FIG. 9



6/7

FIG. 10

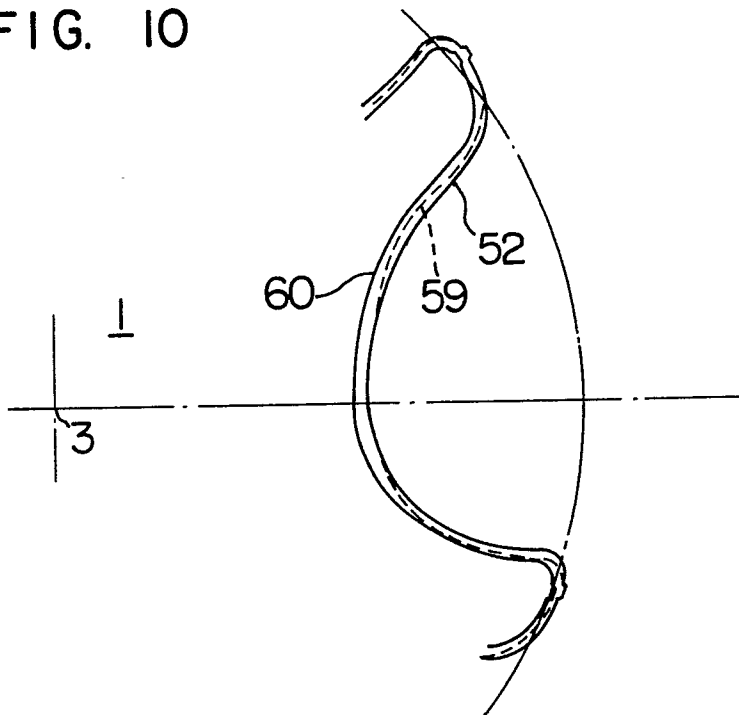
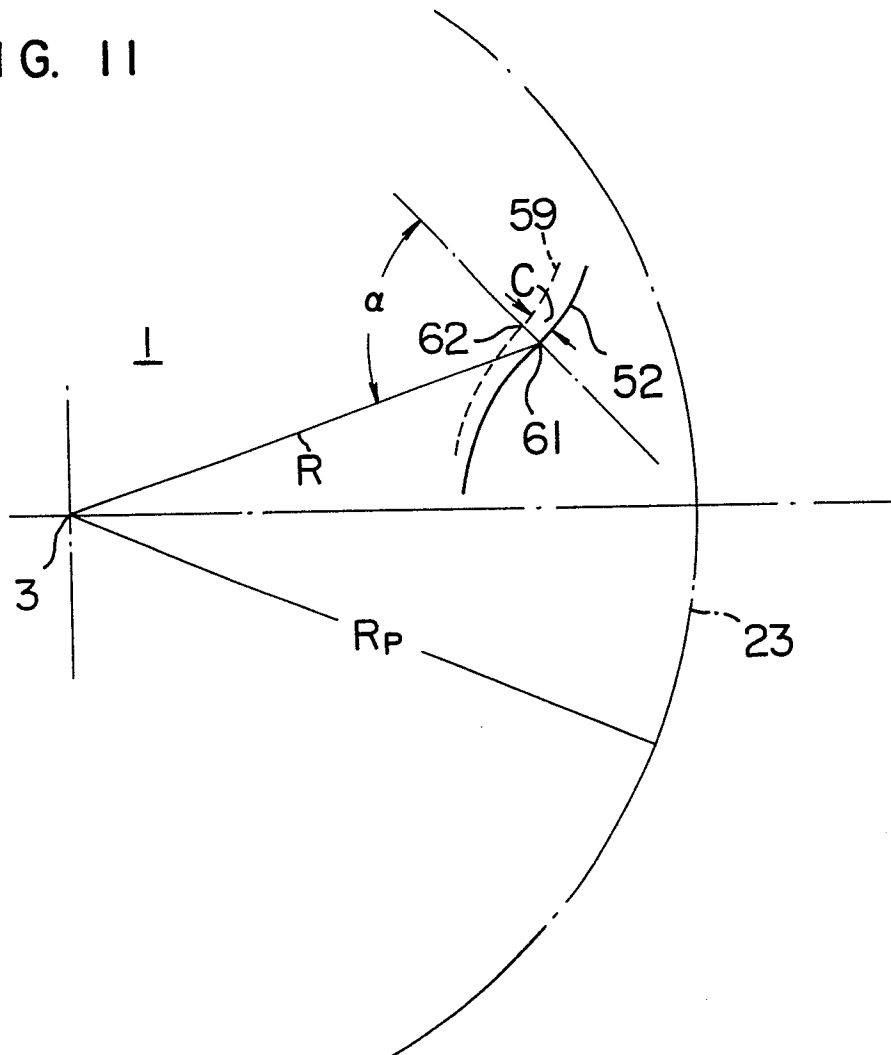


FIG. 11



7/7

FIG. 12

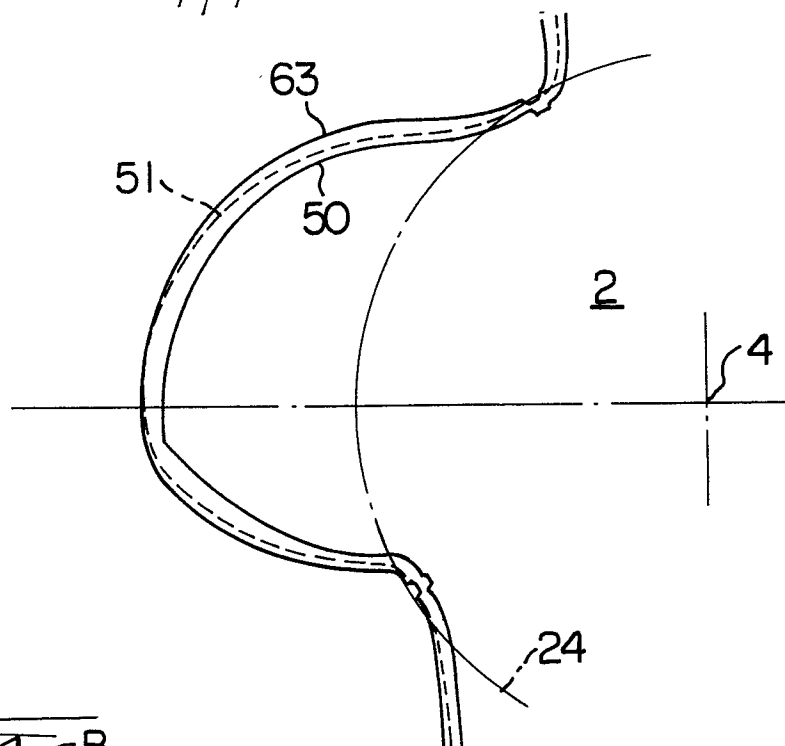


FIG. 14

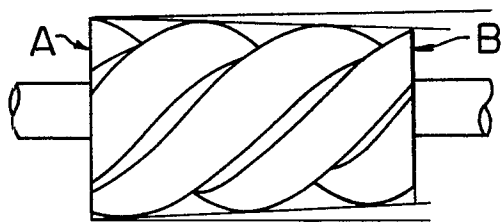
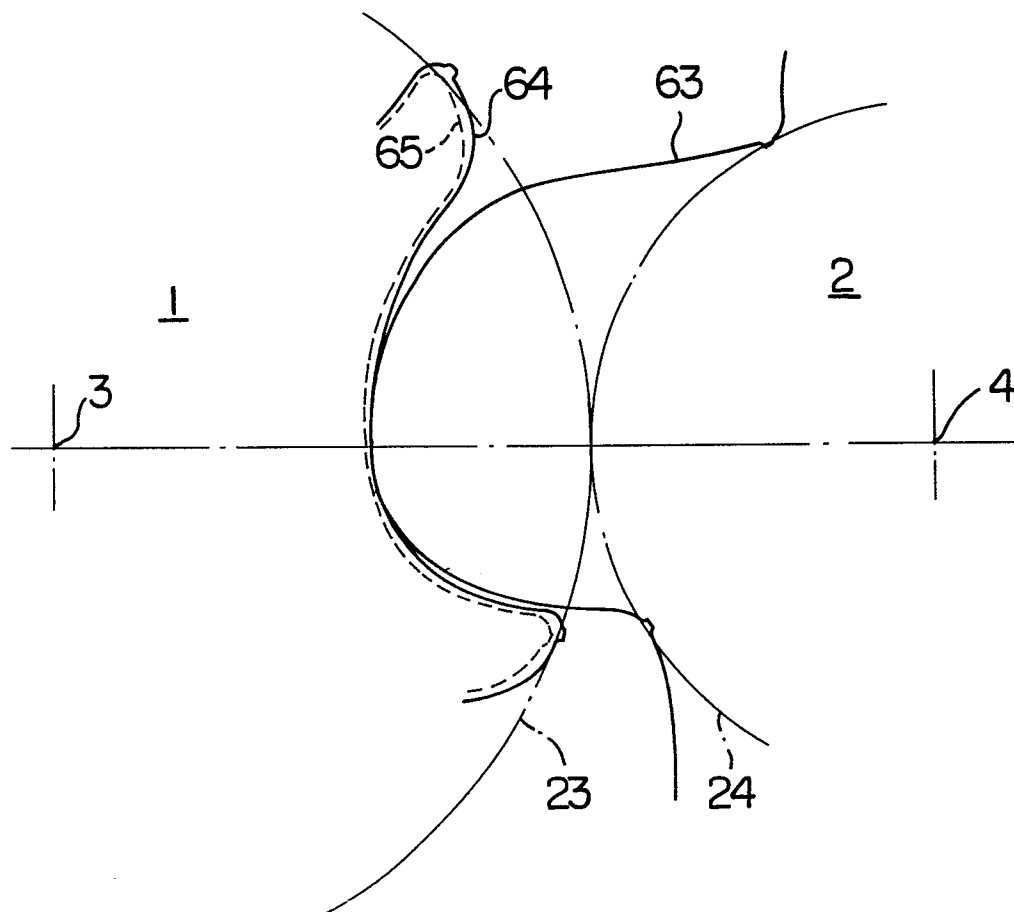


FIG. 13





DOCUMENTS CONSIDERED TO BE RELEVANT			
Category	Citation of document with indication, where appropriate, of relevant passages	Relevant to claim	CLASSIFICATION OF THE APPLICATION (Int. Cl. <sup>3</sup> )
A	EP-A-0 053 342 (HITACHI)  * Abstract; figures *	1-3, 8- 10, 15- 17	F 01 C 1/16
A	GB-A-2 058 928 (HITACHI)  * Abstract; figures *	1, 3, 5, 6, 8, 10 , 12, 13 , 15, 17 , 19, 20	
A	US-A-4 140 445 (SVENSKA ROTOR)  * Column 3, lines 25-63; figure 3; column 4, line 59 - column 5, line 63 *	1, 4, 5, 7, 8, 11 , 14, 15 , 18, 19 , 21	TECHNICAL FIELDS SEARCHED (Int. Cl. <sup>3</sup> )  F 01 C F 04 C
A	FR-A-2 253 930 (DEMAG) * Pages 2, 4; figures *	1, 8, 15	
A	DE-A-1 403 534 (HOWDEN & CO.) * Pages 3, 7, 8; figures *	1, 8, 15	
The present search report has been drawn up for all claims			
Place of search THE HAGUE		Date of completion of the search 24-06-1983	Examiner KAPOULAS T.
<b>CATEGORY OF CITED DOCUMENTS</b>			
X : particularly relevant if taken alone Y : particularly relevant if combined with another document of the same category A : technological background O : non-written disclosure P : intermediate document			
T : theory or principle underlying the invention E : earlier patent document, but published on, or after the filing date D : document cited in the application L : document cited for other reasons  & : member of the same patent family, corresponding document			